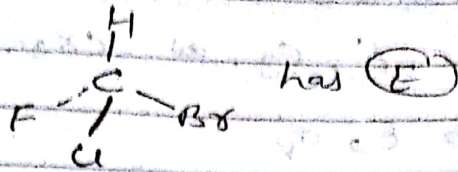


② Identity → It is a symmetry operation without effect. It leaves the molecule unaffected. It is neutral element, as 360° rotation at some molecule as CH_2Br_2 as CH_2Br_2 → no other symmetry element



③ Rotation C_n (proper axis of rotation) → n fold rotation indicate → a rotation through an angle of $360^\circ/n$ → i.e. rotation at same structure

$$C_n^n \equiv E$$

as $H_2O \rightarrow C_2$, $NH_3 \rightarrow C_3$

mirror planes

- σ_h (horizontal) → Plane perpendicular to principal axis
- σ_d (dihedral), σ_v (vertical) → Plane linear with principal axis
- $\sigma_d \rightarrow \sigma$ parallel to C_n & bisecting C_2' axis
- $\sigma_v \rightarrow$ vertical, parallel to principal axis

Short \bar{n}

Elements	operation	Symbol
• Identity	identity	$\rightarrow E$
• Plane of symmetry	[Reflection in a plane]	$\rightarrow \sigma$
• Inver Centre of symmetry	[Inversion of all the atoms through centre of symmetry]	$i = S_2$
• Proper axis	[Rotation by $360^\circ/n$]	$\rightarrow C_n$
Improper axis	[① Rotation by $360^\circ/n$ ② Reflection in plane perpendicular to rotation-axis]	S_n ($n=3$)

Point gr | (B)

Point gr | Symmetry elements (4)

(1) C_1	\longleftrightarrow	E as C_1, B, σ, π
(2) C_2	\longleftrightarrow	E, C_2 as H_2O_2, F_2O_2
(3) C_3	\longleftrightarrow	E, C_3 as CX_3-CY_3
(4) C_s	\longleftrightarrow	E, σ_v
(5) C_{2v}	\longleftrightarrow	$E, C_2, 2\sigma_v$
(6) C_{3v}	\longleftrightarrow	$E, C_3, 3\sigma_v$
(7) $C_{\infty v}$	\longleftrightarrow	E, C_{∞}, σ_v all linear molec
(8) C_{2h}	\longleftrightarrow	E, C_2, σ_h, i
(9) D_{2h}	\longleftrightarrow	$E, 3C_2, 3\sigma, i$
C_{nh}	\longleftrightarrow	E, C_n axis, σ plane, i

(10) C_n (Rotational point gr) \rightarrow

(1) C_1 gr $\rightarrow C_1 \equiv E$
or

Point gr

① C_{nh} point gr \rightarrow

formula $C_{nh} = C_n + 1\sigma_h$
 Total No of elements / operation = $2n$

② C_{nv} point gr \rightarrow

$$C_{nv} = C_n + n\sigma_v$$

Total No of operations = $(2n)$

As of $n=2$, then $C_{2v} = 4 = \underset{\textcircled{1}}{C_2} + \underset{\textcircled{2}}{2\sigma_v} + \underset{\textcircled{1}}{E}$

③ D_{nh} point gr \rightarrow

formula $\rightarrow C_n + nC_2 + n\sigma_v + 1\sigma_h$

No. of operation = $(4n)$

As of $n=2$ then \rightarrow

$$8 = D_{2h} = \underset{\textcircled{1}}{C_2} + \underset{\textcircled{2}}{2C_2} + \underset{\textcircled{2}}{2\sigma_v} + \underset{1}{1\sigma_h} + \underset{1}{1}E + \underset{1}{1}S_2$$

as $BF_3 \overset{\Delta}{\text{h}} D_{3h}$

$$\rightarrow C_3 + 3\sigma_v + 1\sigma_h + 3C_2$$

④ D_{nd} point gr $\rightarrow C_n + nC_2 + n\sigma_d$

No of operations = $(4n)$

$$As \rightarrow 8 = D_{2d} = \underset{\textcircled{1}}{C_2} + \underset{\textcircled{2}}{2C_2} + \underset{\textcircled{2}}{2\sigma_d} + \underset{\textcircled{1}}{1}E + \underset{\textcircled{2}}{1}S_4$$

⑤ C_n point gr $\rightarrow C_n + E$
 No of operations = n

as $C_2 = C_2 + E$
 $C_3 = C_3 + E$

⑥ S_{2n} point gr
 $\rightarrow S_{2n} + C_n + E$
 \rightarrow NO of operation = $2n$
 as $S_4 = S_4 + C_2 + E$
 ② ① ① = 4

⑦ D_n point gr \rightarrow
 $C_n + nC_2$
 \rightarrow NO of operations = $2n$

as $6 = D_3 = C_3 + 3C_2 + E$
 ② ③ ①

⑧ Tetrahedral point gr $\rightarrow CH_4$
 \rightarrow 4 corners
 \rightarrow 6 edges
 \rightarrow 4 triangular faces
 \rightarrow Total NO of operators = 24
 $(8 + 3 + 6 + 6 + 1 = 24)$

- It consists of $\textcircled{3}$ $\textcircled{7}$
- 4 C_3 axis → Passing through each C_3 bond through each corner = 8 operations
 - 3 C_2 axis → Passing through opposite edge or face of cube = 3 operations
 - 3 S_4 → along each C_2 -axis = 6 operations
 - 6 σ_d (dihedral plane) → 6 operations
 - E (1 operation)

$\textcircled{8}$ Octahedral points) → as SF6

- no of operation = 48
- $9 + 8 + 6 + 6 + 8 + 3 + 6 + 1 + 1 = 48$
- 6 corners, 12 edges, 8 triangular faces
- 3 C_4 axis → Passing through opposite corners $\textcircled{9}$
- 4 C_3 axis → Passing through opposite triangular face → $\textcircled{8}$
- 6 C_2 axis → " " edges $\textcircled{6}$
- 3 S_4 axis → along each C_4 axis $\textcircled{6}$
- 4 S_6 " $\textcircled{8}$
- 3 σ_h $\textcircled{3}$
- 6 σ_d $\textcircled{6}$
- 6 σ_d $\textcircled{6}$
- Inversion centre (I)
- Identity (E) → $\textcircled{1}$

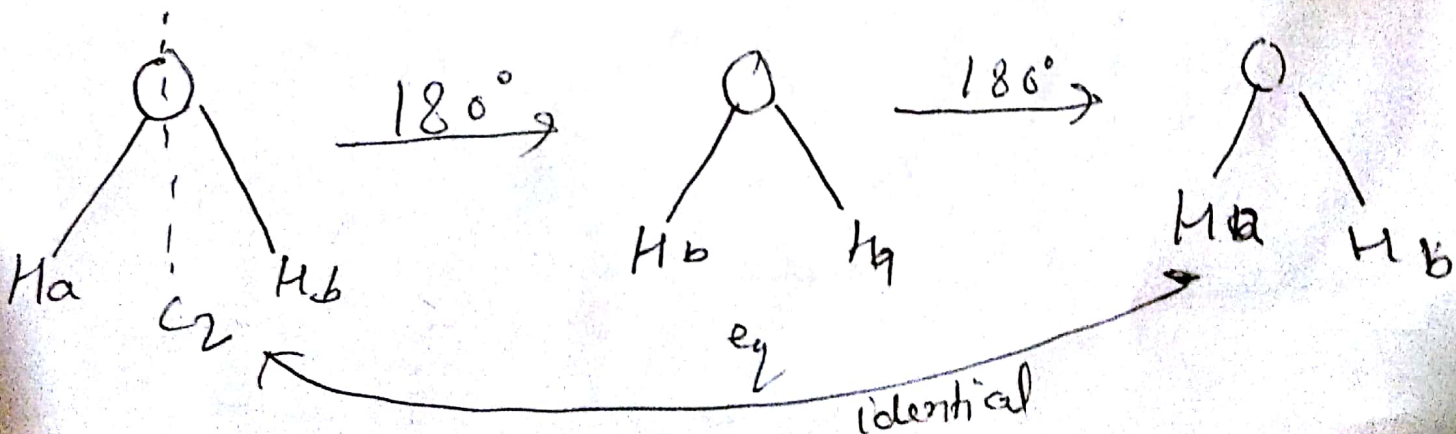
② Axis of Symmetry (C_n) → rotation होता है
 ↳ rotation के बाद equivalent or identical
 स्वर प्राप्त होती है

$$n = \frac{360^\circ}{\theta}$$

↳ यदि $\theta = 180^\circ$

↳ $n = \frac{360^\circ}{180^\circ} = 2$ or C_2

ie 180° के rotation के बाद same configuration
 प्राप्त होता है (A₁) H₂O



①

Point gr

Identity = E

5

- Axis of symmetry \rightarrow Rotation (C_n)
- Plane of symmetry \rightarrow Reflection (σ)
- Centre of symmetry \rightarrow Inversion (i)
- Improper axis \Rightarrow Roto-reflection (S_n)

Symmetry Elements & Symmetry operations

Symmetry elements \rightarrow The symmetry of a molecule is determined by the existence of symmetry operations performed with respect to symmetry elements. It is a geometrical entity.

Symmetry operations \rightarrow operations which leave a object looking the same

To characterize symmetry in a concise way, two sets of symmetry symbols are introduced \rightarrow

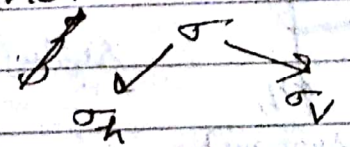
① Schoenflies symbols
used in mainly molecular spectroscopy

② Hermann-Mauguin symbols or International Symbol.

Symmetry elements \rightarrow ⑤ E

- ① Identity
- ② Plane of symmetry (σ i.e. sigma plane)
- ③ Simple or proper axis of symmetry (C_n)
- ④ Center of symmetry or inversion center (i)
- ⑤ Rotation-reflection axis i.e. ~~alt~~ alternating axis of symmetry (S_n) ($\sigma_h \cdot C_n$)

⑥ Plane of symmetry \rightarrow जो एक molecule को two half में divide कर देता है, जो mirror plane है



$\sigma^2 \equiv E$

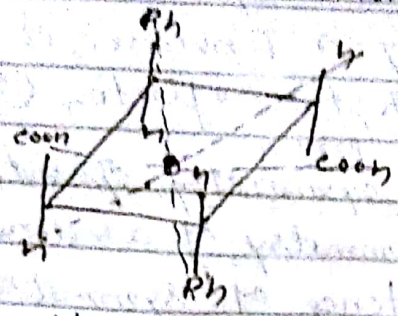
\rightarrow सुविधा के लिए, the principal plane is placed vertically along the z axis i.e. z-axis is principal axis.

σ_h \rightarrow perpendicular to the principal axis horizontal.

σ_v \rightarrow vertical mirror plane to the main axis

σ_d \rightarrow If such a plane bisects the angle b/w a, of rotational axis C_2 , we have a diagonal mirror plane.

(2) center of symmetry (C_i inversion center)
 of all straight lines that can be drawn through the center of the molecule meet identical atoms (or points) at the same distance from the centre.



360°
 or $\frac{360^\circ}{n}$
 n fold axis

(3) alternating or rotation-reflection axis,
 a molecule is said to have an alternating or a rotation reflection axis of symmetry if an arrangement identical to the original is restored when → (i) the molecule is rotated through n degrees about an axis passing through the molecule, & (ii) the rotated molecule is reflected in a mirror that is perpendicular to the axis of rotation in 1st step

